

(11)  $x = 6$

(12) no solution

(13)  $x = -5$

(14)  $x = 4$

(15)  $x = -1$

(16)  $x = -2$

(17)  $x = -3, 6$

(18) no solution

Solve the equation by using the LCD. Check for extraneous solutions.

$$11. \frac{x}{x} \cdot \frac{3}{2} + \frac{1}{x} \cdot \frac{2}{2} = \frac{1+x}{x} + \frac{4}{x}$$

$$\frac{3x}{2x} + \frac{2}{2x} = \frac{x}{x} + \frac{4}{x}$$

$$\frac{3x+2}{2x} = \frac{x+4}{x}$$

$$x(3x+2) = 2x(x+4)$$

$$3x^2 + 2x = 2x^2 + 8x$$

$$x^2 - 6x = 0$$

$$x(x-6) = 0$$

$$x \neq 0 \quad x-6=0$$

$$x=6$$

$$12. \frac{-x+1}{x-1} + 2 \frac{x-1}{x-1} = \frac{1}{x}$$

$$\frac{-x+1}{x-1} + \frac{2(x-1)}{x-1} = \frac{1}{x}$$

$$\frac{-x+1+2x-2}{x-1} = \frac{1}{x}$$

$$\frac{x-1}{x-1} = \frac{1}{x}$$

$$1 = \frac{1}{x}$$

$$x = x$$

no solution

$$13. \frac{x}{x} \cdot 1 + \frac{6}{x} = \frac{2x-4}{x} - 3 \frac{x}{x}$$

$$\frac{x}{x} + \frac{6}{x} = \frac{2x-4}{x} - \frac{3x}{x}$$

$$\frac{x+6}{x} = \frac{2x-4-3x}{x}$$

$$\frac{x+6}{x} = \frac{-x-4}{x}$$

$$x(x+6) = x(-x-4)$$

$$x^2 + 6x = -x^2 - 4x$$

$$2x^2 + 10x = 0$$

$$2x(x+5) = 0$$

$$2x=0 \quad x+5=0$$

$$x \neq 0 \quad x = -5$$

$$14. \frac{6}{x-3} - 4 \frac{x-3}{x-3} = \frac{2}{x-3}$$

$$\frac{6}{x-3} - \frac{4(x-3)}{x-3} = \frac{2}{x-3}$$

$$6 - 4x + 12 = 2$$

$$-4x + 18 = 2$$

$$-4x = -16$$

$$x = 4$$

$$15. \frac{x+3}{x+3} \cdot \frac{4}{x-3} + \frac{2}{x+3} \cdot \frac{x-3}{x-3} = \frac{2x+2}{x^2-9}$$

$$\frac{4(x+3) + 2(x-3)}{(x+3)(x-3)} = \frac{2x+2}{x^2-9}$$

$$\frac{4x+12+2x-6}{x^2-9} = \frac{2x+2}{x^2-9}$$

$$6x+6 = 2x+2$$

$$4x = -4$$

$$x = -1$$

$$16. \frac{x^2}{3x-1} + 2 \frac{x-1}{3x-1} = \frac{2(x-3)}{3x-1}$$

$$\frac{x^2 + 2(3x-1)}{3x-1} = \frac{2x-6}{3x-1}$$

$$x^2 + 6x - 2 = 2x - 6$$

$$x^2 + 4x + 4 = 0$$

$$(x+2)(x+2) = 0$$

$$x+2=0$$

$$x = -2$$

$$17. \frac{2x+1}{2x+1} \cdot \frac{x}{2x-1} - \frac{2}{2x+1} \cdot \frac{2x-1}{2x-1} = \frac{x^2+20}{4x^2-1}$$

$$\frac{x(2x+1) - 2(2x-1)}{(2x+1)(2x-1)} = \frac{x^2+20}{4x^2-1}$$

$$\frac{2x^2+x-4x+2}{4x^2-1} = \frac{x^2+20}{4x^2-1}$$

$$18. \frac{x+6}{x+6} + \frac{5}{x+6} = \frac{6x-1}{x+6}$$

$$\frac{x(x+6) + 5}{(x+6)} = \frac{6x-1}{x+6}$$

$$\frac{2x^2 + x - 4x + 2}{4x^2 - 1} = \frac{x^2 + 20}{4x^2 - 1}$$

$$2x^2 - 3x + 2 = x^2 + 20$$

$$x^2 - 3x - 18 = 0$$

$$(x - 6)(x + 3) = 0$$

$$x - 6 = 0 \quad x + 3 = 0$$

$$x = 6 \quad x = -3$$

$$\frac{(x+6)}{x+6}$$

$$x^2 + 6x + 5 = 6x - 1$$

$$x^2 + 6 = 0$$

no solution