

$$11. \frac{x-2}{x^2-2} + \frac{x}{x^2-2}$$

$$\frac{2(x^2-2)}{(x^2-2)} + \frac{x}{x^2-2}$$

$$\frac{2x^2-4+x}{x^2-2}$$

$$\boxed{\frac{2x^2+x-4}{x^2-2}}$$

Simplify the complex fraction.

$$13. \frac{\frac{x-1}{x-1} \cdot \frac{2}{x} + \frac{3}{x-1} \cdot \frac{x}{x}}{\frac{1}{2x-2}}$$

$$\frac{\frac{2(x-1)}{x(x-1)} + \frac{3(x)}{x(x-1)}}{\frac{1}{2x-2}}$$

$$\frac{\frac{2x-2+3x}{x(x-1)}}{\frac{1}{2(x-1)}}$$

$$= \frac{5x-2}{x(x-1)} \cdot \frac{2(x-1)}{1}$$

$$\boxed{\frac{2(5x-2)}{x}}$$

$$12. \frac{x-2}{x^2+x-12} + \frac{x}{x^2-2x-3}$$

$$\frac{(x+1) \cdot \frac{x-2}{(x+4)(x-3)} + \frac{x}{(x-3)(x+1)} \cdot \frac{(x+4)}{(x+4)}$$

$$\frac{(x+1)(x-2)}{(x+1)(x+4)(x-3)} + \frac{x(x+4)}{(x+1)(x+4)(x-3)}$$

$$\frac{x^2-2x+x-2+x^2+4x}{(x+1)(x+4)(x-3)}$$

$$\frac{2x^2+3x-2}{(x+1)(x+4)(x-3)} = \boxed{\frac{(2x-1)(x+2)}{(x+1)(x+4)(x-3)}}$$

$$14. \frac{\frac{3}{3} \cdot \frac{3}{x+2} + \frac{2}{3} \cdot \frac{x+2}{x+2}}{\frac{x}{x} \cdot \frac{2x}{x+2} - \frac{1}{x} \cdot \frac{x+2}{x+2}}$$

$$= \frac{\frac{9}{3(x+2)} + \frac{2(x+2)}{3(x+2)}}{\frac{2x^2}{x(x+2)} - \frac{(x+2)}{x(x+2)}}$$

$$= \frac{9+2x+4}{3(x+2)} \cdot \frac{x(x+2)}{2x^2-x-2}$$

$$= \frac{2x+13}{3(x+2)} \cdot \frac{x(x+2)}{2x^2-x-2}$$

$$= \boxed{\frac{x(2x+13)}{3(2x^2-x-2)}}$$

$$15. \frac{2x-1}{2x-1} \cdot \frac{5}{4x} - \frac{2 \cdot \frac{2x-1}{2x-1}}{2x-1} \cdot \frac{4x}{4x}$$

$$= \frac{3x}{2x-1} - \frac{2(2x-1)}{2x-1}$$

$$\frac{5(2x-1) - 4x^2}{4x(2x-1)} \cdot \frac{4x}{4x(2x-1)}$$

$$= \frac{3x-4x+2}{2x-1}$$

$$\frac{10x-5-4x^2}{4x(2x-1)}$$

$$= \frac{-x+2}{2x-1} \cdot \frac{4x(2x-1)}{-4x^2+10x-5}$$

$$= \frac{(x-2) \cdot 4x}{(4x^2-10x+5)}$$

$$= \boxed{\frac{4x(x-2)}{4x^2-10x+5}}$$

In Exercises 16 and 17, use the following information.

Doctors Over a twenty year period the number of doctors of medicine M (in thousands) in the United States can be approximated by $M = \frac{28,390 + 693t}{85 - t}$ where $t = 0$ represents 1980. The number of doctors of osteopathy B (in thousands) can be approximated by $B = \frac{776 - 12t}{55 - 2t}$.

16. Write an expression for the total number T of doctors of medicine (MD) and doctors of osteopathy (DO). Simplify the result.

$$T = \frac{28,390 + 693t}{85 - t} + \frac{776 - 12t}{55 - 2t}$$

17. How many MDs did the United States have in 1990? how many DOs?

$$M = \frac{28,390 + 693(10)}{85 - 10} \quad t=10 \quad B = \frac{776 - 12(10)}{55 - 2(10)}$$

17. How many MDS did the United States have in 1990? How many DOS?

$$M = \frac{28,390 + 693(t)}{85 - t}$$

$$\approx 471,000 \text{ MDS}$$

$t = 10$

$$B = \frac{776 - 12(t)}{55 - 2(t)}$$

$$\approx 19,000 \text{ DOS}$$

$$\textcircled{11} \quad 2x^2 + x - 4$$

$$\textcircled{12} \quad \frac{(2x-1)(x+2)}{(x+1)(x+4)(x-3)}$$

$$\textcircled{13} \quad \frac{2(5x-2)}{x}$$

$$\textcircled{14} \quad \frac{x(2x+13)}{3(2x^2-x-2)}$$

$$\textcircled{15} \quad \frac{4x(x-2)}{4x^2-10x+5}$$

$$\textcircled{17} \quad \approx 471,000 \text{ MDS}$$
$$\approx 19,000 \text{ DOS}$$