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③ Law of cosines ④ Law of sines ⑤ Law of sines

⑥ Law of cosines ⑦ Law of sines

$$\textcircled{36} \begin{array}{l} C = 64^\circ \\ a = 19.2 \\ c = 18.1 \end{array}$$

$$\textcircled{37} \begin{array}{l} A = 45^\circ \\ b = 25.2 \\ c = 15.3 \end{array}$$

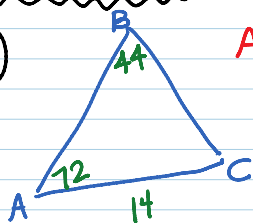
$$\textcircled{38} \begin{array}{l} A = 34.3^\circ \\ B = 80.7^\circ \\ c = 19.3 \end{array}$$

$$\textcircled{39} \begin{array}{l} A = 68.2^\circ \\ C = 21.8^\circ \\ b = 16.2 \end{array}$$

$$\textcircled{40} \begin{array}{l} A = 81^\circ \\ B = 59^\circ \\ a = 41.5 \end{array} \text{ OR } \begin{array}{l} A = 19.0^\circ \\ B = 121.0^\circ \\ a = 13.7 \end{array}$$

Solutions

③⑥

AAS \Rightarrow Law of Sines
1 Δ

$$\begin{array}{l} C = 180 - (44 + 72) \\ C = 64^\circ \end{array}$$

$$\frac{\sin 72}{a} = \frac{\sin 44}{14}$$

$$\frac{\sin 64}{c} = \frac{\sin 44}{14}$$

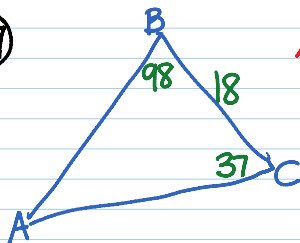
$$\frac{a \sin 44}{\sin 44} = \frac{14 \sin 72}{\sin 44}$$

$$\frac{c \sin 44}{\sin 44} = \frac{14 \sin 64}{\sin 44}$$

$$a = 19.2$$

$$c = 18.1$$

③⑦

ASA \Rightarrow Law of Sines
1 Δ

$$\begin{array}{l} A = 180 - (98 + 37) \\ A = 45^\circ \end{array}$$

$$\frac{\sin 98}{b} = \frac{\sin 45}{18}$$

$$\frac{\sin 37}{c} = \frac{\sin 45}{18}$$

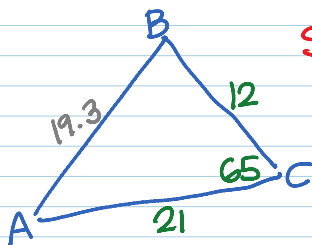
$$b = \frac{18 \sin 98}{\sin 45}$$

$$c = \frac{18 \sin 37}{\sin 45}$$

$$b = 25.2$$

$$c = 15.3$$

③⑧

SAS \Rightarrow Law of Cosines
1 Δ

$$\begin{array}{l} c^2 = a^2 + b^2 - 2ab \cos C \\ c^2 = 12^2 + 21^2 - 2(12)(21) \cos 65 \\ c^2 = 372.0 \\ c = 19.3 \end{array}$$

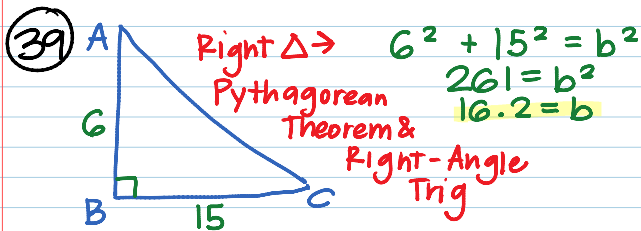
$$\frac{\sin A}{12} = \frac{\sin 65}{19.3}$$

$$\begin{array}{l} B = 180 - (34.3 + 65) \\ B = 80.7^\circ \end{array}$$

$$\sin A = \frac{12 \sin 65}{19.3}$$

$$\frac{19.3}{\sin A} = .56$$

$$A = 34.3^\circ$$



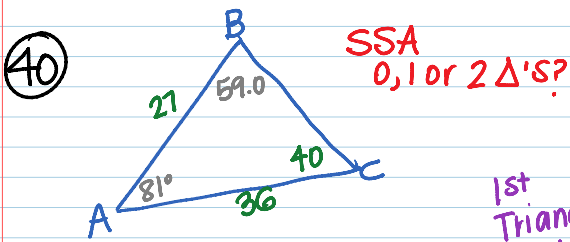
$$\tan A = \frac{15}{6}$$

$$A = \tan^{-1}\left(\frac{5}{2}\right)$$

$$A = 68.2^\circ$$

$$C = 180 - (90 + 68.2)$$

$$C = 21.8^\circ$$



1st Triangle

$$\frac{\sin B}{36} = \frac{\sin 40}{27}$$

$$\frac{27 \sin B}{27} = \frac{36 \sin 40}{27}$$

$$\sin B = .86$$

$$B = \sin^{-1}(.86)$$

$$B = 59.0$$

$$A = 180 - (59 + 40)$$

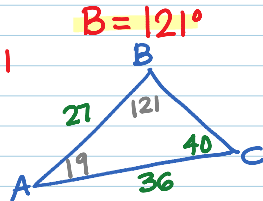
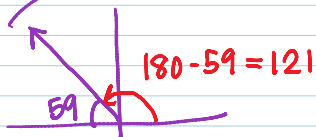
$$A = 81^\circ$$

$$\frac{\sin 81}{a} = \frac{\sin 40}{27}$$

$$a = \frac{27 \sin 81}{\sin 40}$$

$$a = 41.5$$

2nd triangle



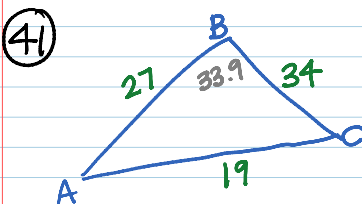
$$A = 180 - (121 + 40)$$

$$A = 19^\circ$$

$$\frac{\sin 19}{a} = \frac{\sin 40}{27}$$

$$a = \frac{27 \sin 19}{\sin 40}$$

$$a = 13.7$$



$$b^2 = a^2 + c^2 - 2ac \cos B$$

$$19^2 = 34^2 + 27^2 - 2(34 \times 27) \cos B$$

$$361 = 1885 - 1836 \cos B$$

$$\frac{-1885 - 1885}{-1836} = \frac{-1836 \cos B}{-1836}$$

$$.83 = \cos B$$

$$\cos^{-1}(.83) = B$$

$$33.9^\circ = B$$

$$\frac{\sin C}{27} = \frac{\sin 33.9}{19}$$

$$\sin C = \frac{27 \sin 33.9}{19}$$

$$\sin C = .79$$

$$A = 180 - (33.9 + 52.4)$$

$$A = 93.7^\circ$$

$$C = \sin^{-1}(.79)$$

$$C = 52.4^\circ$$